



Coimisiún na Scrúduithe Stáit  
State Examinations Commission

**LEAVING CERTIFICATE 2010**

**MARKING SCHEME**

**APPLIED MATHEMATICS**

**HIGHER LEVEL**



## General Guidelines

1 Penalties of three types are applied to candidates' work as follows:

Slips - numerical slips S(-1)

Blunders - mathematical errors B(-3)

Misreading - if not serious M(-1)

Serious blunder or omission or misreading which oversimplifies:  
- award the attempt mark only.

Attempt marks are awarded as follows: 5 (att 2).

2 The marking scheme shows one correct solution to each question.  
In many cases there are other equally valid methods.

1. (a) A car is travelling at a uniform speed of  $14 \text{ m s}^{-1}$  when the driver notices a traffic light turning red 98 m ahead.

Find the minimum constant deceleration required to stop the car at the traffic light,

- (i) if the driver immediately applies the brake  
(ii) if the driver hesitates for 1 second before applying the brake.

(i) 
$$v^2 = u^2 + 2fs$$

$$0 = 14^2 + 2f(98)$$

$$196f = -196$$

$$\Rightarrow f = -1 \text{ m s}^{-2}$$

(ii) 
$$s = ut + \frac{1}{2}ft^2$$

$$s = 14(1) + 0$$

$$s = 14$$

$$v^2 = u^2 + 2fs$$

$$0 = 14^2 + 2f(98 - 14)$$

$$0 = 14^2 + 168f$$

$$f = \frac{-196}{168}$$

$$= -\frac{7}{6} \text{ or } -1.17 \text{ m s}^{-2}$$

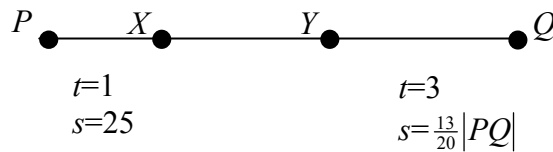
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1. (b) A particle passes  $P$  with speed  $20 \text{ m s}^{-1}$  and moves in a straight line to  $Q$  with uniform acceleration.

In the first second of its motion after passing  $P$  it travels 25 m.

In the last 3 seconds of its motion before reaching  $Q$  it travels  $\frac{13}{20}$  of  $|PQ|$ .

Find the distance from  $P$  to  $Q$ .



$$\begin{aligned}
 PX \quad s &= ut + \frac{1}{2}ft^2 \\
 25 &= 20(1) + \frac{1}{2}f(1)^2 \\
 5 &= \frac{1}{2}f \\
 \Rightarrow f &= 10
 \end{aligned}$$

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$$\begin{aligned}
 PY \quad s &= ut + \frac{1}{2}ft^2 \\
 \frac{7}{20}|PQ| &= 20(t+1) + 5(t+1)^2 \\
 &= 5t^2 + 30t + 25
 \end{aligned}$$

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$$\begin{aligned}
 PQ \quad s &= ut + \frac{1}{2}ft^2 \\
 |PQ| &= 20(t+4) + 5(t+4)^2 \\
 &= 5t^2 + 60t + 160
 \end{aligned}$$

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$$\begin{aligned}
 \frac{7}{20}|PQ| &= 5t^2 + 30t + 25 \\
 \frac{7}{20}(5t^2 + 60t + 160) &= 5t^2 + 30t + 25 \\
 65t^2 + 180t - 620 &= 0 \\
 \Rightarrow t &= 2
 \end{aligned}$$

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$$\begin{aligned}
 |PQ| &= 20(6) + 5(6)^2 \\
 &= 300 \text{ m}
 \end{aligned}$$

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2. (a) Two particles, A and B, start initially from points with position vectors  $6\vec{i} - 14\vec{j}$  and  $3\vec{i} - 2\vec{j}$  respectively. The velocities of A and B are constant and equal to  $4\vec{i} - 3\vec{j}$  and  $5\vec{i} - 7\vec{j}$  respectively.

(i) Find the velocity of B relative to A.

(ii) Show that the particles collide.

$$\begin{aligned}
 \vec{V}_A &= 4\vec{i} - 3\vec{j} \\
 \vec{V}_B &= 5\vec{i} - 7\vec{j} \\
 \vec{V}_{BA} &= \vec{V}_B - \vec{V}_A \\
 &= \vec{i} - 4\vec{j}
 \end{aligned}$$

magnitude =  $\sqrt{17} \text{ m s}^{-1}$  or slope =  $-4$   
 or direction = East  $75.58^\circ$  South

$$\begin{aligned}
 \vec{R}_A &= 6\vec{i} - 14\vec{j} \\
 \vec{R}_B &= 3\vec{i} - 2\vec{j} \\
 \vec{R}_{AB} &= \vec{R}_A - \vec{R}_B \\
 &= 3\vec{i} - 12\vec{j} \text{ or } 3(\vec{i} - 4\vec{j})
 \end{aligned}$$

slope =  $-4$   
 or direction = East  $75.58^\circ$  South

$\Rightarrow$  The particles collide

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- 2 (b) When a motor-cyclist travels along a straight road from South to North at a constant speed of  $12.5 \text{ m s}^{-1}$  the wind appears to her to come from a direction North  $45^\circ$  East.

When she returns along the same road at the same constant speed, the wind appears to come from a direction South  $45^\circ$  East.

Find the magnitude and direction of the velocity of the wind.

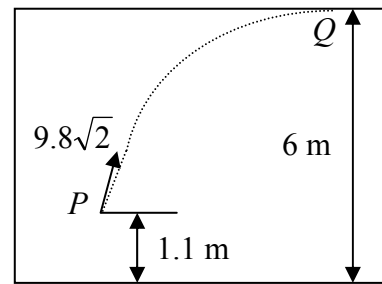
$\vec{V}_M = 0\vec{i} + 12.5\vec{j}$	5	
$\vec{V}_{WM} = -x\vec{i} - x\vec{j}$		
$\vec{V}_W = \vec{V}_{WM} + \vec{V}_M$	5	
$= -x\vec{i} + (12.5 - x)\vec{j}$		
$\vec{V}_M = 0\vec{i} - 12.5\vec{j}$	5	
$\vec{V}_{WM} = -y\vec{i} + y\vec{j}$		
$\vec{V}_W = \vec{V}_{WM} + \vec{V}_M$	5	
$= -y\vec{i} + (y - 12.5)\vec{j}$		
$\vec{V}_W = \vec{V}_W$	5	
$\Rightarrow x = y \text{ and } 12.5 - x = y - 12.5$		
$\Rightarrow x = y = 12.5$		
$\vec{V}_W = -12.5\vec{i} + 0\vec{j}$	5	
magnitude = $12.5 \text{ m s}^{-1}$		
direction = West		

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3. (a) In a room of height 6 m, a ball is projected from a point  $P$ .

$P$  is 1.1 m above the floor.

The velocity of projection is  $9.8\sqrt{2}$  m s<sup>-1</sup> at an angle of  $45^\circ$  to the horizontal.



The ball strikes the ceiling at  $Q$  without first striking a wall.  
Find the length of the straight line  $PQ$ .

$$9.8\sqrt{2} \sin 45^\circ t - \frac{1}{2}gt^2 = 4.9$$

$$4.9t^2 - 9.8t + 4.9 = 0$$

$$t^2 - 2t + 1 = 0$$

$$t = 1$$

$$\begin{aligned} r_x &= 9.8\sqrt{2} \cos 45^\circ t \\ &= 9.8 \end{aligned}$$

$$\begin{aligned} |PQ| &= \sqrt{9.8^2 + 4.9^2} \\ &= 4.9\sqrt{5} \text{ or } 10.96 \text{ m} \end{aligned}$$

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3 (b)

A particle is projected up an inclined plane with initial speed  $80 \text{ m s}^{-1}$ . The line of projection makes an angle of  $30^\circ$  with the inclined plane and the plane is inclined at an angle  $\theta$  to the horizontal. The plane of projection is vertical and contains the line of greatest slope.

The particle strikes the plane at an angle of  $\tan^{-1} \frac{2}{\sqrt{3}}$ .

Find (i) the value of  $\theta$

(ii) the speed with which the particle strikes the plane.

(i)  $r_j = 0$

$$0 = 80 \sin 30 \cdot t - \frac{1}{2} g \cos \theta t^2$$

$$\Rightarrow t = \frac{80}{g \cos \theta}$$

$$v_i = 80 \cos 30 - g \sin \theta \left( \frac{80}{g \cos \theta} \right)$$

$$= 40\sqrt{3} - 80 \tan \theta$$

$$v_j = 80 \sin 30 - g \cos \theta \left( \frac{80}{g \cos \theta} \right)$$

$$= -40$$

$$\tan \ell = \frac{-v_j}{v_i}$$

$$\frac{2}{\sqrt{3}} = \frac{40}{40\sqrt{3} - 80 \tan \theta}$$

$$\tan \theta = \frac{\sqrt{3}}{4} \Rightarrow \theta = 23.4^\circ$$

(ii)  $v_i = 20\sqrt{3}$

$v_j = -40$

$$\text{speed} = \sqrt{(20\sqrt{3})^2 + (-40)^2}$$

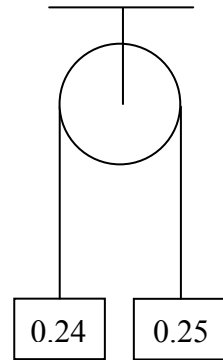
$$= 20\sqrt{7} \text{ or } 52.9 \text{ m s}^{-1}$$

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4. (a) Two particles of masses 0.24 kg and 0.25 kg are connected by a light inextensible string passing over a small, smooth, fixed pulley.

The system is released from rest.

- Find (i) the tension in the string  
(ii) the speed of the two masses when the 0.25 kg mass has descended 1.6 m.



$$(i) \quad 0.25g - T = 0.25f$$

$$T - 0.24g = 0.24f$$

$$0.01g = 0.49f$$

$$f = 0.2$$

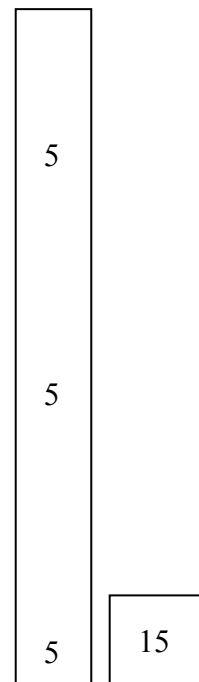
$$\Rightarrow T = 2.4 \text{ N}$$

$$(ii) \quad v^2 = u^2 + 2fs$$

$$= 0 + 2(0.2)(1.6)$$

$$v = \sqrt{0.64}$$

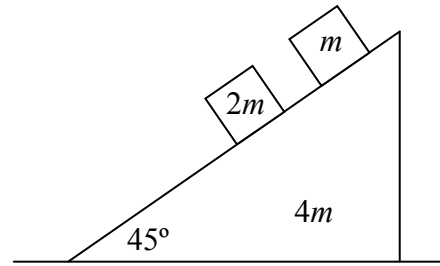
$$v = 0.8 \text{ m s}^{-1}$$



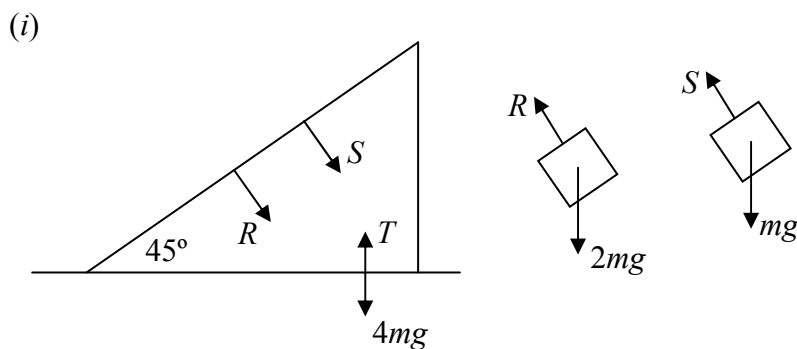
- 4 (b) A smooth wedge of mass  $4m$  and slope  $45^\circ$  rests on a smooth horizontal surface.

Particles of mass  $2m$  and  $m$  are placed on the smooth inclined face of the wedge.

The system is released from rest.



- (i) Show, on separate diagrams, the forces acting on the wedge and on the particles.
- (ii) Find the acceleration of the wedge.



(ii)

$$2m \quad 2mg \cos 45 - R = 2mf \sin 45$$

$$R = \sqrt{2}(mg - mf)$$

$$m \quad mg \cos 45 - S = mf \sin 45$$

$$S = \frac{1}{\sqrt{2}}(mg - mf)$$

$$4m \quad S \sin 45 + R \sin 45 = 4mf$$

$$\frac{1}{2}(mg - mf) + (mg - mf) = 4mf$$

$$3mg - 3mf = 8mf$$

$$f = \frac{3g}{11} \text{ or } 2.67 \text{ m s}^{-2}$$

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5. (a) A sphere, of mass  $m$  and speed  $u$ , impinges directly on a stationary sphere of mass  $3m$ .

The coefficient of restitution between the spheres is  $e$ .

- (i) Find, in terms of  $u$  and  $e$ , the speed of each sphere after the collision.  
(ii) If  $e = \frac{1}{4}$ , find the percentage loss in kinetic energy due to the collision.

(i) PCM  $m(u) + 3m(0) = mv_1 + 3mv_2$

NEL  $v_1 - v_2 = -e(u - 0)$

$$\left. \begin{aligned} v_1 &= \frac{u(1-3e)}{4} \\ v_2 &= \frac{u(1+e)}{4} \end{aligned} \right\}$$

(ii)

$$e = \frac{1}{4}$$

$$\Rightarrow v_1 = \frac{u}{16} \text{ and } v_2 = \frac{5u}{16}$$

$$\text{K.E. before} = \frac{1}{2}mu^2$$

$$\begin{aligned} \text{K.E. after} &= \frac{1}{2}mv_1^2 + \frac{1}{2}(3m)v_2^2 \\ &= \frac{1}{2}m\left(\frac{u}{16}\right)^2 + \frac{1}{2}(3m)\left(\frac{5u}{16}\right)^2 \\ &= \frac{76mu^2}{512} \quad \text{or} \quad \frac{19mu^2}{128} \end{aligned}$$

$$\text{Loss in KE} = \frac{1}{2}mu^2 - \frac{19mu^2}{128} = \frac{45mu^2}{128}$$

$$\text{Percentage loss in KE} = \frac{\frac{45mu^2}{128}}{\frac{1}{2}mu^2}(100) = 70.3\%$$

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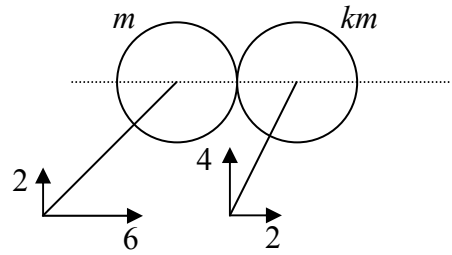
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- (b) A smooth sphere, of mass  $m$ , moving with velocity  $6\vec{i} + 2\vec{j}$  collides with a smooth sphere, of mass  $km$ , moving with velocity  $2\vec{i} + 4\vec{j}$  on a smooth horizontal table.



After the collision the spheres move in parallel directions.

The coefficient of restitution between the spheres is  $e$ .

- (i) Find  $e$  in terms of  $k$ .  
(ii) Prove that  $k \geq \frac{1}{3}$ .

(i) PCM  $m(6) + km(2) = mv_1 + kmv_2$   
NEL  $v_1 - v_2 = -e(6 - 2)$

$$v_1 = \frac{6 + 2k - 4ek}{k + 1}$$

$$v_2 = \frac{6 + 4e + 2k}{k + 1}$$

parallel directions  $\Rightarrow$  slopes are equal

$$\frac{2}{v_1} = \frac{4}{v_2}$$

$$v_2 = 2v_1$$

$$\frac{6 + 4e + 2k}{k + 1} = \frac{2(6 + 2k - 4ek)}{k + 1}$$

$$3 + 2e + k = 6 + 2k - 4ek$$

$$e = \frac{3 + k}{2 + 4k}$$

(ii)

$$e \leq 1$$

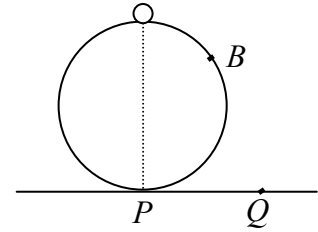
$$\frac{3 + k}{2 + 4k} \leq 1$$

$$3 + k \leq 2 + 4k$$

$$k \geq \frac{1}{3}$$

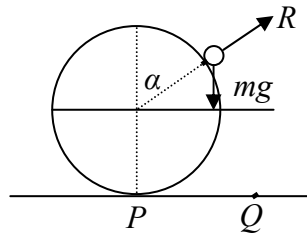
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6. (a) A particle of mass  $m$  kg lies on the top of a smooth sphere of radius 2 m. The sphere is fixed on a horizontal table at  $P$ .



The particle is slightly displaced and slides down the sphere. The particle leaves the sphere at  $B$  and strikes the table at  $Q$ .

- Find (i) the speed of the particle at  $B$   
(ii) the speed of the particle on striking the table at  $Q$ .



$$(i) \quad mg \cos \alpha - R = \frac{mv^2}{2}$$

$$R = 0 \quad \Rightarrow v^2 = 2g \cos \alpha$$

$$\frac{1}{2}mv^2 = mg(2 - 2 \cos \alpha)$$

$$\frac{1}{2}m(2g \cos \alpha) = mg(2 - 2 \cos \alpha)$$

$$\Rightarrow \cos \alpha = \frac{2}{3}$$

$$\Rightarrow v = \sqrt{\frac{4g}{3}} \text{ m s}^{-1}$$

$$(ii) \quad \text{Total energy at } Q = \text{Total energy at } B$$

$$\frac{1}{2}mv_1^2 = \frac{1}{2}mv^2 + mg(2 + 2 \cos \alpha)$$

$$\frac{1}{2}mv_1^2 = \frac{1}{2}m\left(\frac{4g}{3}\right) + mg\left(2 + \frac{4}{3}\right)$$

$$\Rightarrow v_1 = \sqrt{8g} \text{ m s}^{-1}$$

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- 6 (b) A particle moves with simple harmonic motion of amplitude 0.75 m.  
The period of the motion is 4 s.

- Find (i) the maximum speed of the particle  
(ii) the time taken by the particle to move from the position of maximum speed to a position at which its speed is half its maximum value.

(i) Period = 4

$$\frac{2\pi}{\omega} = 4$$

$$\omega = \frac{\pi}{2}$$

$$v_{\max} = \omega a$$

$$= \frac{\pi}{2} \left( \frac{3}{4} \right)$$

$$= \frac{3\pi}{8} \text{ m s}^{-1}$$

(ii)  $\frac{1}{2} v_{\max} = \frac{3\pi}{16}$

$$v^2 = \omega^2 (a^2 - x^2)$$

$$\left( \frac{3\pi}{16} \right)^2 = \left( \frac{\pi}{2} \right)^2 \left( \left( \frac{3}{4} \right)^2 - x^2 \right)$$

$$\Rightarrow x = \frac{3\sqrt{3}}{8}$$

$$x = a \cos \omega t$$

$$\frac{3\sqrt{3}}{8} = \frac{3}{4} \cos \left( \frac{\pi}{2} t \right)$$

$$\Rightarrow t = \frac{1}{3}$$

$$\text{time} = 1 - \frac{1}{3} = \frac{2}{3} \text{ s.}$$

$$\frac{3\sqrt{3}}{8} = \frac{3}{4} \sin \left( \frac{\pi}{2} t \right)$$

$$\Rightarrow t = \frac{2}{3} \text{ s.}$$

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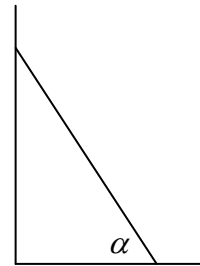
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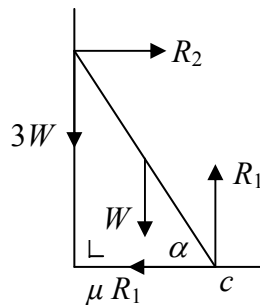
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7. (a) One end of a uniform ladder, of weight  $W$ , rests against a smooth vertical wall, and the other end rests on rough horizontal ground. The coefficient of friction between the ladder and the ground is  $\mu$ . The ladder makes an angle  $\alpha$  with the horizontal and is in a vertical plane which is perpendicular to the wall.



Show that a person of weight  $3W$  can safely climb to the top of the ladder if

$$\mu > \frac{7}{8 \tan \alpha}.$$



horizontal  $R_2 = \mu R_1$

vertical  $R_1 = 4W$

$$\Rightarrow R_2 = 4\mu W$$

moments about  $c$  :

$$R_2 (\ell \sin \alpha) = W \left( \frac{1}{2} \ell \cos \alpha \right) + 3W (\ell \cos \alpha)$$

$$R_2 (\tan \alpha) = \frac{7W}{2}$$

$$4\mu W (\tan \alpha) = \frac{7W}{2}$$

$$\Rightarrow \mu = \frac{7}{8 \tan \alpha}$$

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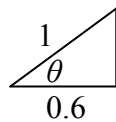
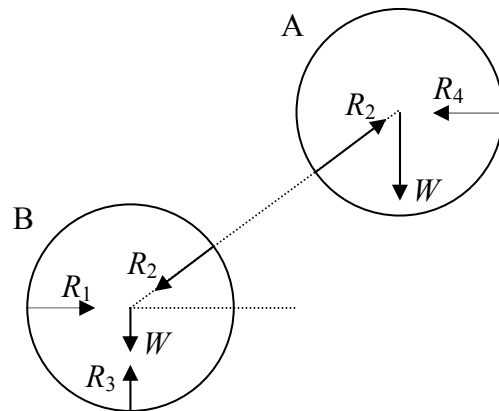
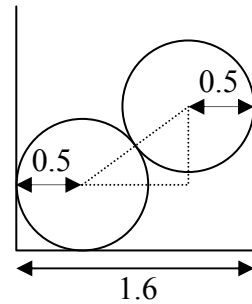
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7. (b) Two uniform smooth spheres each of weight  $W$  and radius  $0.5$  m, rest inside a hollow cylinder of diameter  $1.6$  m.

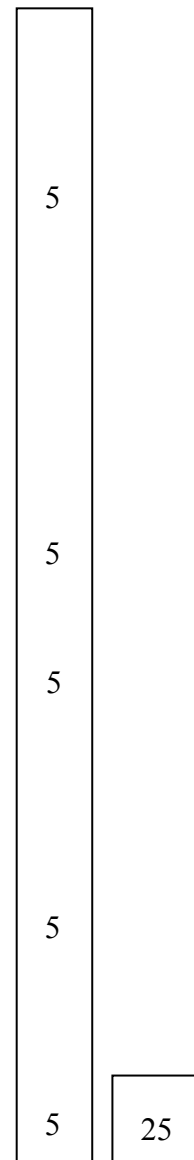
The cylinder is fixed with its base horizontal.

- (i) Show on separate diagrams the forces acting on each sphere.
- (ii) Find, in terms of  $W$ , the reaction between the two spheres.
- (iii) Find, in terms of  $W$ , the reaction between the lower sphere and the base of the cylinder.



$$\cos \theta = \frac{3}{5} \Rightarrow \sin \theta = \frac{4}{5}$$

- (ii) Sphere A  $R_2 \sin \theta = W$   
 $R_2 \left( \frac{4}{5} \right) = W$   
 $R_2 = \frac{5W}{4}$
- (iii) Sphere B  $R_3 = R_2 \sin \theta + W$   
 $R_3 = W + W$   
 $R_3 = 2W$



8. (a) Prove that the moment of inertia of a uniform circular disc, of mass  $m$  and radius  $r$ , about an axis through its centre perpendicular to its plane is  $\frac{1}{2} m r^2$ .

Let  $M$  = mass per unit area

$$\text{mass of element} = M\{2\pi x dx\}$$

$$\text{moment of inertia of the element} = M\{2\pi x dx\}x^2$$

$$\text{moment of inertia of the disc} = 2\pi M \int_0^r x^3 dx$$

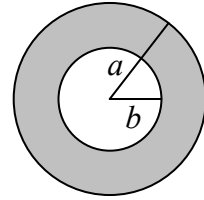
$$= 2\pi M \left[ \frac{x^4}{4} \right]_0^r$$

$$= 2\pi M \frac{r^4}{4}$$

$$= \frac{1}{2} m r^2$$

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8. (b) An annulus is created when a central hole of radius  $b$  is removed from a uniform circular disc of radius  $a$ .



The mass of the annulus (shaded area) is  $M$ .

- (i) Show that the moment of inertia of the annulus about an axis through its centre and perpendicular to its plane is  $\frac{M(a^2 + b^2)}{2}$ .
- (ii) The annulus rolls, from rest, down an incline of  $30^\circ$ . Find its angular velocity, in terms of  $g$ ,  $a$  and  $b$ , when it has rolled a distance  $\frac{a}{2}$ .

(i) moment of inertia of annulus =  $2\pi M_1 \int_b^a x^3 dx$  5

$$= 2\pi M_1 \left[ \frac{x^4}{4} \right]_b^a$$

$$= 2\pi \frac{M}{\pi(a^2 - b^2)} \frac{(a^4 - b^4)}{4}$$

$$= \frac{M(a^2 + b^2)}{2}$$

(ii) Gain in KE = Loss in PE 5

$$\frac{1}{2} I \omega^2 + \frac{1}{2} M v^2 = M g h$$

$$\frac{1}{2} I \omega^2 + \frac{1}{2} M (a \omega)^2 = M g \left( \frac{a}{2} \sin 30 \right)$$

$$\frac{1}{2} \left\{ \frac{M(a^2 + b^2)}{2} \right\} \omega^2 + \frac{1}{2} M (a \omega)^2 = M g \left( \frac{a}{4} \right)$$

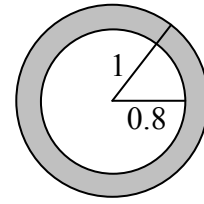
$$\omega = \sqrt{\frac{g a}{3 a^2 + b^2}}$$

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9. (a) State the Principle of Archimedes.

A buoy in the form of a hollow spherical shell of external radius 1 m and internal radius 0.8 m floats in water with 61% of its volume immersed.



Find the density of the material of the shell.

**Principle of Archimedes**

$$\begin{aligned}
 B &= \rho V g \\
 &= 1000 \left\{ \frac{61}{100} \left( \frac{4}{3} \pi (1)^3 \right) \right\} g \\
 &= 610 \left( \frac{4}{3} \pi \right) g
 \end{aligned}$$

$$\begin{aligned}
 W &= \rho V g \\
 &= \rho \left\{ \frac{4}{3} \pi (1)^3 - \frac{4}{3} \pi (0.8)^3 \right\} g \\
 &= 0.488 \rho \left( \frac{4}{3} \pi \right) g
 \end{aligned}$$

$$W = B$$

$$0.488 \rho \left( \frac{4}{3} \pi \right) g = 610 \left( \frac{4}{3} \pi \right) g$$

$$\rho = \frac{610}{0.488} = 1250 \text{ kg m}^{-3}$$

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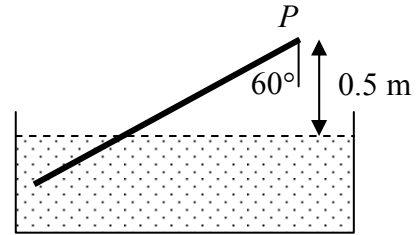
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- 9 (b) A uniform rod, of length 1.5 m and weight  $W$ , is freely hinged at a point  $P$ .

The rod is free to move about a horizontal axis through  $P$ .  
The other end of the rod is immersed in water.



The point  $P$  is 0.5 m above the surface of the water.

The rod is in equilibrium and is inclined at an angle of  $60^\circ$  to the vertical.

- Find (i) the relative density of the rod  
(ii) the reaction at the hinge in terms of  $W$ .

(i) length of immersed part =  $x$

$$(1.5 - x)\cos 60 = \frac{1}{2}$$

$$\Rightarrow x = \frac{1}{2}$$

moments about  $P$  :

$$B\left(\frac{5}{4}\right)\sin 60 = W\left(\frac{3}{4}\right)\sin 60$$

and  $B = \frac{\frac{1}{3}W(1)}{s} = \frac{W}{3s}$

$$\frac{5W}{3s} = 3W$$

$$s = \frac{5}{9}$$

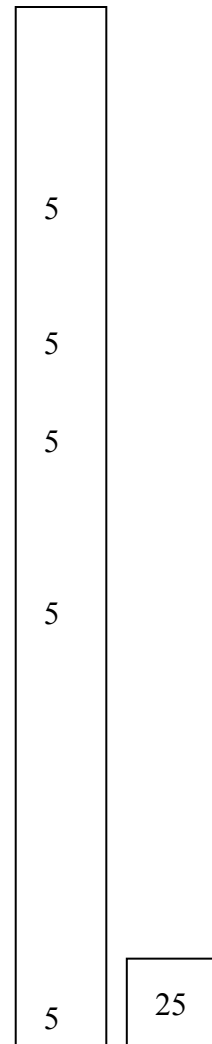
(ii)

$$B = \frac{W}{3s} = \frac{3W}{5}$$

$$B + R = W$$

$$\frac{3W}{5} + R = W$$

$$\Rightarrow R = \frac{2W}{5}$$



10. (a) Solve the differential equation

$$y \frac{dy}{dx} = x + xy^2$$

given that  $y = 0$  when  $x = 0$ .

$$y \frac{dy}{dx} = x + xy^2$$

$$\frac{dy}{dx} = \frac{x(1+y^2)}{y}$$

$$\int \frac{y}{1+y^2} dy = \int x dx$$

$$\frac{1}{2} \ln(1+y^2) = \frac{1}{2} x^2 + C$$

$$y = 0, x = 0$$

$$\Rightarrow C = 0$$

$$\frac{1}{2} \ln(1+y^2) = \frac{1}{2} x^2$$

$$1+y^2 = e^{x^2}$$

$$\Rightarrow y = \sqrt{e^{x^2} - 1}$$

5

5

5

5

20

- 10 (b) The acceleration of a cyclist freewheeling down a slight hill is

$$0.12 - 0.0006v^2 \text{ m s}^{-2}$$

where the velocity  $v$  is in metres per second.

The cyclist starts from rest at the top of the hill.

- Find (i) the speed of the cyclist after travelling 120 m down the hill  
(ii) the time taken by the cyclist to travel the 120 m if his average speed is  $2.65 \text{ m s}^{-1}$ .

(i)	$v \frac{dv}{dx} = 0.12 - 0.0006v^2$		5
	$\int_0^v \frac{v}{0.12 - 0.0006v^2} dv = \int_0^{120} dx$		5
	$\left[ -\frac{1}{0.0012} \ln(0.12 - 0.0006v^2) \right]_0^v = [x]_0^{120}$		5
	$-\frac{1}{0.0012} \ln(0.12 - 0.0006v^2) + \frac{1}{0.0012} \ln(0.12) = 120$		5
	$\frac{1}{0.0012} \ln\left(\frac{0.12}{0.12 - 0.0006v^2}\right) = 120$		
	$\ln\left(\frac{0.12}{0.12 - 0.0006v^2}\right) = 0.144$		5
	$\frac{0.12}{0.12 - 0.0006v^2} = e^{0.144} = 1.155$		
	$\Rightarrow v = 5.18 \text{ m s}^{-1}$		5
(ii)	average speed = $\frac{\text{distance}}{\text{time}}$		
	$2.65 = \frac{120}{t}$		
	$\Rightarrow t = 45.3 \text{ s}$		5

30
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### Marcanna Breise as ucht freagairt trí Ghaeilge

Ba chóir marcanna de réir an ghnáthrata a bhronnadh ar iarrthóirí nach ngnóthaíonn níos mó ná 75% d'iomlán na marcanna don pháipéar. Ba chóir freisin an marc bónais sin a shlánú **síos**.

Déantar an cinneadh agus an ríomhaireacht faoin marc bónais i gcás gach páipéir ar leithligh.

Is é 5% an gnáthrata agus is é 300 iomlán na marcanna don pháipéar. Mar sin, bain úsáid as an ghnáthrata 5% i gcás iarrthóirí a ghnóthaíonn 225 marc nó níos lú, e.g.  $198 \text{ marc} \times 5\% = 9.9 \Rightarrow \text{bónas} = 9 \text{ marc}$ .

Má ghnóthaíonn an t-iarrthóir níos mó ná 225 marc, ríomhtar an bónas de réir na foirmle  $[300 - \text{bunmharc}] \times 15\%$ , agus an marc bónais sin a shlánú **síos**. In ionad an ríomhaireacht sin a dhéanamh, is féidir úsáid a bhaint as an tábla thíos.

Bunmharc	Marc Bónais
226	11
227 – 233	10
234 – 240	9
241 – 246	8
247 – 253	7
254 – 260	6
261 – 266	5
267 – 273	4
274 – 280	3
281 – 286	2
287 – 293	1
294 – 300	0









